## **Boundary Elements**

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Class: Office Hours:

Textbook: NO Textbook Recommended Reading:

## **CONTENTS**

- 1) Introduction. Boundary Elements and Finite Elements. Historical development of the BEM.
- 2) Preliminary Mathematical Concepts. The Gauss-Green theorem. The divergence theorem of Gauss. Green's second identity. The Dirac delta function.
- The BEM for Potential Problems in Two Dimensions. Fundamental solution. The direct BEM for the Laplace and the Poisson equation. Transformation of the domain integrals to boundary integrals.
- 4) The BEM for potential problems in anisotropic bodies.
- 5) Numerical Implementation of the BEM. The BEM with constant boundary elements.
- 6) The Dual Reciprocity Method for Poisson's equation. Computer program for solving the Laplace equation with constant boundary elements.
- 7) Domains with multiple boundaries. The method of subdomains. Boundary Element Technology. Linear elements. Higher order elements. Near-singular integrals.
- 8) Applications. Torsion of non-circular bars. Deflection of elastic membranes. Bending of simply supported plates. Heat transfer problems. Fluid flow problems.
- 9) The BEM for Two-Dimensional Elastostatic Problems. Equations of plane elasticity. Betti's reciprocal identity. Fundamental solution. Integral representation of the solution. Boundary integral equations. Numerical solution of the boundary integral equations. Body forces.
- 10) Computer program for solving the plane elastostatic problem with constant boundary elements.